

CA Final - AFM Formula Sheet

Risk Management

Variance :
$$\frac{\sum (x-\bar{x})^2}{n}$$

where x is observation, n is number of observations and \bar{x} is the mean of observations.

Standard Deviation : $\sigma =$

√Variance

Covariance: $\sum \frac{(x-\overline{x})(y-\overline{y})}{n}$

Correlation : $\rho = \frac{Cov(X,Y)}{\sigma_x \sigma_y}$

Where, Cov (X,Y) is covariance

 σ is Standard Deviation

Standard Deviation of portfolio:

$$\sigma_{\rm p} = \sqrt{\sigma_1^2 + \sigma_2^2 + \left(2(\sigma_1\sigma_2 \,\rho)\right)}$$

Where σ_1 is standard deviation of 1st security and σ_2 is standard deviation of 2nd security in Rupee terms

Or,

$$\sqrt{\frac{w_1^2\sigma_1^2 + w_2^2\sigma_2^2 + }{\left(2(w_1w_2\sigma_1\sigma_2 \rho)\right)}}$$

Where w₁ & w₂ are the weights of respective securities & SDs are in %

Value at Risk (VAR):

 $\sigma_p x$ Portfolio Value x Cumulative Z score x $\sqrt{N \ Days}$

Where, Z score indicates how many standard deviation away from mean

Market Capitalisation: Total number of shares × Market price of share

Advanced Capital Budgeting Decisions

Cash Flow after tax:

 $(R-C) \times (1-T) + D \times T$ Where,

R is Revenue, C is Cost, T is Tax rate and D is Depreciation.

Rn = Rr * (1 + P) [For Absolute]

R_n is Nominal return,

R_r is Real return,

P is Expected Inflation Rate (%).

(1+Rn) = (1+Rr)*(1+P) [For Rates]

R_n is Nominal rate of return (%) R_r is Real rate of return (%) P is Expected Inflation Rate (%).

Statistical Methods of Incorporating Risk in Capital Budgeting:

1. Probability weighted Cashflows:

Expected Value: ∑*Pi NCFi*

Where, Pi is the probability and NCF_i is the Net Cash flows.

2. Variance : $\frac{\sum (x-\bar{x})^2}{n}$

 $= \sum Pi (x - \overline{X})^2$

Where x is Net cash flow, \bar{x} is the expected net cashflow and Pi is the probability.

Variance as per Hillers Model:

$$\sigma^2 = \sum (1+r)^{-2i} \sigma^2_i$$

Where,

1+r is the discount rate and i is the time period.

- 3. Standard Deviation : $\sqrt{\sigma^2} = \sqrt{Variance}$
- 4. Coefficient of Variation :
 Standard Deviation
 Expected Cashflow

Conventional Methods of Incorporating Risk in Capital Budgeting:

1. Risk Adjusted Discount Rate

RADR =
$$R_f + \beta(R_m - R_f)$$
 or
RADR = $R_f + R_f$ Risk Premium

Where, R_m is Market return R_f is Risk free rate of return and β is beta

2. Certainty Equivalent

(
$$\alpha$$
): $\frac{Certain\ Cashflows}{Expected\ Risky\ Cashflows}$

NPV=
$$\sum \frac{\alpha \times NCF}{(1+k)^n}$$
 - Initial Investment

Where, α is Risk Adjustment factor, NCF is net cash flow without risk adjustment, K is Risk free rate and n is number of periods.

Expected Net Present Value (Multiple Periods):

ENPV = Sum of Present Value of Cashflows calculated Individually – Initial Investment

Replacement Decision:

Step 1: Net Cash flow = Cost of new Machine – (tax saving + market value of old machine)

[usually a negative value]

Step 2: (Change in Sales +/- Change in Operating Cost – Change in Depreciation) × (1- Tax) + Change in

Depreciation **Or**

(Change in Sales +/- Change in Operating Cost) ×(1- Tax) + (Change in Depreciation × Tax)

Step 3: Present Value of Cashflows = Present Value of Yearly Cash Flows

+ Present Value of Salvage

Step 4: NPV = Step 1 [cash outflow i.e -ve value] + Step 3 [cash inflow i.e +ve value]

Optimum Replacement Cycle:

Equivalent Annual Cost (EAC) = Present Value of Cash Outflow (PVCF)

Present Value Annuity Factor(PVAF)

Adjusted Present Value:

Base Case NPV (on unlevered cost of capital) + PV of tax benefits on interest

Profitability Index =

Discount Cash inflow

Initial Investment

Security Analysis

Gordon's Dividend Growth Model:

Current Stock Price(P) =
$$\frac{D1}{k-g}$$

Where.

D₁ is value of next year dividend, k is the minimum rate of return, g is growth rate of dividend.

PE Multiple : Current Market Price
Earnings per share

Confidence Index:

Avg yield on high grade bond

Avg yield on low grade bond

Arithmetic Moving Average:

AMA $_{n, t}$ = 1/n [$P_t + P_{t-1} + ... + P_{t-(n-1)}$] Where,

N is number of total periods and t is period.

Exponential Moving Average:

$$EMA_{t} = aP_{t} + (1-a) (EMA_{t-1})$$

Where, a(exponent) =
$$\frac{2}{n+1}$$

N Is number of days, P_t is price of today and EMA_{t-1} is previous day EMA.

For Run tests,

Mean =
$$\frac{2n1n2}{n1+n2} + 1$$
,

where n1 and n2 are sign changes,

Variance =

$$(n1+n2)(n1+n2)(n1+n2-1)$$

Number of runs: Runs lies between $\mu \pm t(\sigma)$, where

t is distribution with degree of freedom (DoF) & DoF – Number of Runs – 1

Valuation of Debentures and Bonds

Bond Value:

$$P_0 = \sum_{t=1}^{n} \frac{C}{(1+y)^t} + \frac{M}{(1+y)^n}$$

Or,

 $P_0 = C (PVIFA_{y,n}) + M (PVIF_{y,n})$ Where,

 P_0 = Bond price; n = Maturity period; C = Coupon; y = YTM; M = Maturity value

Alternate Formula:

$$P_{o} = \frac{C}{y} x \left[1 - \frac{1}{(1+y)^{n}} \right] + \frac{M}{(1+y)^{n}}$$

Bond value (when coupon payments are semi-annual):

$$P_{o} = \sum_{t=1}^{2n} \frac{\frac{C}{2}}{(1 + \frac{y}{2})^{t}} + \frac{M}{(1 + \frac{y}{2})^{2n}}$$

Where,

2n = Maturity period expressed in terms of half-yearly periods; C/2 = Semi-annual coupon; y/2 = Discount rate applicable for half-year period

Bond Basic Value (between 2 coupon dates):

Present Value of (A + Coupon)

- Accrued Interest

Where,

A = Bond price calculated as on next coupon date after payment of coupon

Present value of (A + Coupon) A + Coupon

$$(1 + \frac{\text{Req. YTM}}{\text{No. of periods}})^{\frac{\text{Time until next coupon}}{\text{Total coupon period}}}$$

Accrued Interest

$$= Face Value x \frac{Coupon rate}{No. of periods} x$$

Time elapsed
Total coupon period

Current Yield: Current market price

Yield To Maturity (YTM):

$$LR + \frac{NPV \text{ at } LR}{NPV \text{ at } LR - NPV \text{ at } HR} \text{ x (HR - LR)}$$

Where.

LR = Lower Rate; HR = Higher Rate

YTM (Approximate Formula):

$$\frac{C \pm \frac{(F-P)}{n}}{\frac{F+P}{2}}$$

Where,

C is coupon, F is face value, P is market price of bond/issue Price, n is years to maturity

Yield To Call:

$$P_{o} = \sum_{t=1}^{n} \frac{C}{(1+y)^{t}} + \frac{\text{Call price}}{(1+y)^{n}}$$

Where y is Yield to Call and n is Call period

Yield To Put:

$$P_{o} = \sum_{t=1}^{n} \frac{C}{(1+y)^{t}} + \frac{Put \, price}{(1+y)^{n}}$$

Where y is Yield to Put and n is Put period

Macaulay Duration:

$$\frac{\sum_{t=1}^{n} \frac{t \, x \, c}{(1+i)^{t}} + \, \frac{n \, x \, M}{(1+i)^{n}}}{P}$$

Where, t is Time; c is Coupon; l is Interest rate; P is Principal; n is Maturity and M is Maturity value

Or

$$\frac{1+y}{y} - \frac{(1+y) + t(c-y)}{C((1+y)^t - 1) + y}$$

Where, Y is yield to maturity

Modified Duration:

$$= - \frac{\text{Macaulay Duration}}{(1 + \frac{\text{YTM}}{n})}$$

Where,

YTM is Yield to Maturity; n is Number of compounding periods per year Or,

$$\frac{\frac{C}{y^2} \left(1 - \frac{1}{(1+y)^n} \right) + \frac{n x \left(M - \frac{C}{y} \right)}{(1+y)^{n+1}}}{P}$$

Convexity adjustment:

$$C^* \times \Delta y^2 \times 100$$

Where.

C* is Convexity formula; Δy is Change in yield for which calculation is done

Convexity Formula :
$$\frac{V_+ + V_- - 2V_0}{2V_0 (\Delta y)^2}$$

Where, V_+ is Price of Bond if yield increases by Δy

 V_- = Price of Bond if yield decreases by Δy

 V_0 = Initial Price of bond; Δy = Change in Yield

Alternate Formula:

$$\frac{\sum_{t=1}^{n}\frac{t(t+1)C}{(1+y)^{n+2}}+\frac{n(n+1)M}{(1+y)^{n+2}}}{P}$$

In simple terms,

$$\begin{split} \text{Convexity} &= \frac{1}{P \ (1+y)^2} \\ &+ \sum_{t=1}^{n} \frac{CF_t \ x \ t \ x \ (t+1)}{(1+y)^t} \end{split}$$

Conversion Value of Debenture:

Price per equity share x Converted no. of shares per debenture

Value of Warrant : $(MP - E) \times n$ Where,

MP is Current Market Price of Share E is Exercise Price of Warrant n is No. of equity shares convertible with one warrant

Yield on Treasury Bills:

$$\frac{FV-Issue\ Price}{Issue\ Price}\ x\ \frac{365}{Maturity}$$

Yield on Commercial Bills/ Certificate of Deposit/ Commercial Paper:

$$\frac{FV - Sale Value}{Sale Value} \times \frac{365}{Maturity}$$

Dirty Price = Clean Price + Accrued Interest

Start Proceeds in Repo

Nominal Value x
$$\frac{\text{Dirty Price}}{100}$$
 x $\frac{100 - \text{Initial Margin}}{100}$

Repayment at Maturity in Repo

Start Proceeds x (1 + Repo Rate x
$$\frac{\text{No, of days}}{360}$$
)

Valuation Equities

Expected Return:

$$(\mathbf{R}_{\mathbf{x}}) = \mathbf{R}_{\mathbf{f}} + \beta_{\mathbf{x}} (\mathbf{R}_{\mathbf{m}} - \mathbf{R}_{\mathbf{f}})$$

Where.

 R_x is expected return on equity R_f is risk-free rate of return β_x is beta of "x" R_m is expected return of market

Equity Risk Premium:

$$(R_x - R_f) = \beta_x (R_m - R_f)$$

Equity Valuation for a holding period of one year

$$P_0 = \frac{D_1 + P_1}{1 + K_e}$$

Where,

 D_1 – Dividend at the end of year 1, P_1 -Price at the end of Year 1 & K_e – Cost of Equity.

Valuation of Equity - Zero Growth

$$P_0 = \frac{D}{K_e}$$

Where, D is Dividend at the end of year 1.

Valuation of Equity – Constant Growth

$$P_0 = \frac{D_1}{K_e - g}$$

Where, $D_1 = D_0$ (1+g), g is growth rate

Valuation of Equity – Two Stage Growth

$$P_0 = \left[\frac{D_0(1+g_1)}{(1+K_e)} + \frac{D_0(1+g_1)^2}{(1+k_e)^2} + \dots \right]$$

$$+ \frac{D_0(1+g_1)^n}{(1+k_e)^n} + \frac{P_n}{(1+k_e)^n}$$

$$P_n = \frac{D_0(1+g_1)^n(1+g_2)}{(K_e - g_2)}$$

Where,

 D_0 is Dividend Just Paid, g_1 is Finite or Super Growth Rate g_2 is Normal Growth Rate K_e is Req. Rate of Return on Equity P_n is Price of share at the end of Super Growth.

H Model

$$P_0 = \frac{D_0 X \frac{t}{2} X (g_S - g_L)}{(K_e - g_L)} + \frac{D_0 (1 + g_L)}{(K_e - g_L)}$$

Where,

 g_s is super normal growth rate g_L is normal growth t is time period

Gordon's Model (Earnings Approach)

$$P_0 = \frac{EPS_1 (1-b)}{(K_e - br)}$$

Where.

P₀ is Price per share b is Retention ratio r is Return on Equity br is Growth Rate (g)

Gordon's Model (Dividend Approach)

$$P_0 = \frac{D_1}{(K_e - br)}$$

Where,

D1 is dividend at the end of yr 1

Earnings Growth Model

$$P_0 = \frac{E_1}{(ROE - g)}$$

Walter's Mode

$$P_0 = \frac{D_0 + (E-D)\frac{1}{K_e}}{(K_e)}$$

Where, E is earning per share and D is dividend per share for the just concluded year

PE or Multiple Approach

Value of an Equity Share = EPS X PE Ratio

Enterprise Value (EV)

$$EV = \frac{FCFF}{K - g}$$

Where.

FCFF is Free cash flow to firm k is Weighted Average cost of Capital g is Growth rate

Theoretical Ex-Right Price (TERP)

$$TERP = \frac{nP_0 + S}{n + n_1}$$

Where,

n is Number of existing equity shares, P_0 is Price of Share Pre-Right Issue, S is Subscription amount raised from Right Issue &

n₁ is No. of new shares offered

Value of Right

$$Value = \frac{TERP - S}{n}$$

Value of Preference Share:

$$\frac{D_1}{(1+r)^1} + \frac{D_2}{(1+r)^2} + \dots + \frac{D_n + Maturity \ Value}{(1+r)^n}$$

Where.

D₁ is Dividend at the end of Year 1 D₂ is Dividend at the end of Year 2 D_n is Dividend at the end of Year n r – Cost of Preference Shares

Portfolio Management

Expected Return:

$$(\overline{X}) = \sum_{i=1}^{n} X_i p(X_i)$$

Where.

 X_i is Possible Returns of a security, P (X_i) is Related probability &

 \overline{X} is Expected Return

Variance:

$$(\sigma^2) = \sum_{i=1}^{n} (X_i - \overline{X})^2 . p(X_i)$$

Where, σ^2 is Variance

Standard Deviation:

$$\mathsf{SD} = \sqrt{\mathsf{variance}} = \sqrt{\sigma^2} = \sqrt{\frac{\sum_{i=1}^n \; (\mathsf{X}_i - \overline{\mathsf{X}})^2}{n}}$$

Covariance:

$$Cov(X,Y) = \sum_{i=1}^{n} (X_i - \overline{X}) (Y_i - \overline{Y}) / n$$

Where,

X is security 1

 \overline{X} is Mean of security 1

Y is security 2

 \overline{Y} is Mean of security 2

n is no. of observations

Correlation Coefficient

$$r_{XY} = \frac{Cov(X, Y)}{\sigma_X. \, \sigma_Y}$$

Where,

 σ_X is standard deviation of X σ_Y is standard deviation of Y

Beta Under Correlation Method

$$\beta = \frac{r_{im}\sigma_i}{\sigma_m} \text{ or } \frac{\text{Cov(i,m)}}{(\sigma_m)^2}$$

Where,

 β is Beta (degree of dependency of returns / ri

 σi – standard deviation of Individual security return

 σm is standard deviation of market return

r is correlation of individual security return (i) and market return (m)

Beta Under Regression Method

$$\beta = \frac{(n\sum xy - \sum x\sum y)}{n\sum x^2 - (\sum x)^2}$$
Or,

$$\beta = \frac{\sum xy - n \overline{x} \overline{y}}{\sum x^2 - n \overline{x}^2}$$

where,

x is independent market return y is dependent stock return

Beta (Slope of line):

$$y = \alpha + \beta x$$

Where,

 α – alpha, intercept value β —Beta, Slope of the line

Portfolio Return:

$$E(R)_p = \sum R_i w_i$$

Where,

 $E(R)_n$ is Portfolio Return R_i is Return on Stock w_i is Weightage of stock in the portfolio

Portfolio Risk:

$$(\sigma p)^2 = w_i^2 \cdot (\sigma_i)^2 + w_j^2 \cdot (\sigma_j)^2 + 2\sigma_i \sigma_j r_{ij} w_i w_j$$

=
$$w_i^2 \cdot (\sigma_i)^2 + w_j^2 \cdot (\sigma_j)^2 + 2Cov(i, j)w_iw_i$$

Where,

i is security 1 & j is security 2 σp is Portfolio risk

 $(\sigma p)^2$ is Portfolio variance

 σ_i is Standard deviation of security 1 σ_i is Standard deviation of security 2 w_i is Weight of security 1 in portfolio w_i is Weight of security 2 in portfolio r_{ii} is correlation between security 1 and 2

Portfolio Risk with different correlation coefficient:

when r is 0, (σ_p) $= \sqrt{w_1^2 \cdot (\sigma_1)^2 + w_2^2 (\sigma_2)^2}$

when r is + 1, $(\sigma_p) = (w_1 \sigma_1 + w_2 \sigma_2)$

when r is -1, $(\sigma_n) = (w_1\sigma_1 - w_2\sigma_2)$

Covariance:

$$Cov(x, y) = r_{xy} . \sigma_x \sigma_y$$

Where,

 r_{xy} – correlation between x and y

Standard Deviation of portfolio:

$$\sigma_{p}^{2} = \sum_{i=1}^{n} \sum_{i=1}^{n} x_{i} x_{j} \cdot r_{ij} \cdot \sigma_{i} \cdot \sigma_{j}$$

$$\sigma_p^2 = \sum_{i=1}^n \sum_{j=1}^n x_i x_j . \sigma_{ij}$$

 x_i : weightage of security 1 in portfolio x_i : weightage of security 2 in portfolio r_{ij} is correlation between security 1 and 2

Variance of portfolio for 3 Securities:

$$\sigma^{2} = \left[2\sigma_{y}\sigma_{z}w_{y}w_{z}r_{yz}\right] + \left[2\sigma_{x}\sigma_{y}w_{x}w_{y}r_{xy}\right] + \left[2\sigma_{x}\sigma_{z}w_{x}w_{z}r_{xz}\right] + \left[(\sigma_{x})^{2}(w_{x})^{2} + \left(\sigma_{y}\right)^{2}(w_{y})^{2} + \left(\sigma_{z}\right)^{2}(w_{z})^{2}\right]$$

Where, x, y & z are Security 1, 2 & 3 respectively

Slope of Capital Market Line (CML):

$$\frac{R_m - R_f}{\sigma_m}$$

Where,

 R_m is Market return R_f is Risk free rate of return σ_m is Market risk (SD of market) Slope is reward per unit of risk borne

Expected return of the portfolio (using CML):

$$E(R_{p)} = \ R_f + \Big(\frac{R_m - R_f}{\sigma_m}\Big).\, \sigma_p$$

Where, σ_p is Portfolio risk

Expected return of the portfolio (using CAPM):

$$E(R) = R_f + \beta(R_m - R_f)$$

Expected return of the stock -**Sharpe Model:**

$$R_i = \alpha_i + \beta_i R_m + \epsilon_i$$

Where,

 R_i is Expected return on a security i α_i is intercept of the straight line or alpha co-efficient

 β_i is slope of straight line or beta coefficient

 R_m is rate of return on market index ϵ_i is error term

Expected risk of the stock - Sharpe Model:

$$(\sigma_i)^2 = (\beta_i)^2.(\sigma_m)^2 + (\sigma_{\varepsilon_i})^2$$

Where.

 $(\sigma_i)^2$ is variance of the security β_i is slope of straight line or beta coefficient

 $(\sigma_m)^2$ is market variance $(\sigma_{\epsilon_i})^2$ is Variance of errors

Covariance between securities -**Sharpe Model:**

$$(\sigma_{ij}) = (\beta_i) \cdot (\beta_j) (\sigma_m)^2$$

Risk (SD) of portfolio - Sharpe Model:

$$\left|\left(\sigma_{p}\right)^{2} = \left[\sum_{i=1}^{n} x_{i} \beta_{i}\right]^{2} \cdot (\sigma_{m})^{2}$$

$$+ \left[\sum_{i=1}^{n} (x_i)^2 (\sigma_{\epsilon_i})^2 \right]$$

Return of the portfolio – Sharpe Model:

$$E = \sum_{i=1}^n x_i (\alpha_i + \beta_i R_m)$$

Alpha of the portfolio:

$$\alpha_p = \sum_{i=1}^n x_i \alpha_i$$

Where,

 x_i is weightage of 'x' security in portfolio

 $lpha_i$ is intercept of the straight line or alpha co-efficient

Beta of the portfolio:

$$\beta_{p} = \sum_{i=1}^{n} w_{i} \beta_{i}$$

Expected return using SML:

$$E_R = \ R_f + \sigma_{im} \left[\frac{R_m - R_f}{(\sigma_m)^2} \right]$$

Expected return - Arbitrage Pricing

theory : $E_R = R_f + \lambda_1 \beta_1 + \lambda_2 \beta_2 ... \lambda_n \beta_n$ Or,

$$\begin{split} E_{R} &= R_{f} + (AV_{1} - EV_{1})\beta_{1} \\ &+ (AV_{2} \\ &- EV_{2}) \beta_{2} (AV_{n} \\ &- EV_{n})\beta_{n} \end{split}$$

Where, λ *is* Risk premium for the factors like GDP, inflation, interest rate, etc

 $(AV_n - EV_n)$ – Surprise Factor due to change in Value of Factor

Weight to achieve Minimum Variance Portfolio:

$$W_A = \frac{\left[\left. \sigma_B^{\, 2} - r_{AB} \sigma_A \sigma_B \right] \right.}{\left. \sigma_A^{\, 2} + \sigma_B^{\, 2} - 2 r_{AB} \sigma_A \sigma_B \right]}$$

Relationship of weight of securities in Minimum Variance Portfolio:

WB = 1 - WA

Sharpe 's Optimal Portfolio:

Calculation of cutoff point (C*):

$$\sigma_m^2 \cdot \sum_{i=1}^n \frac{(R_i - R_f)\beta_i}{{\sigma_{ei}}^2}$$

$$1 + \sigma_{\rm m}^2 \sum_{i=1}^{n} \frac{{\beta_i}^2}{{\sigma_{\rm ei}}^2}$$

Highest C value is taken as cut off point (C*)

Calculation of weights:

$$\frac{Z_i}{\sum_{i=1}^n z_i}$$

Where,
$$Z_i = \frac{\beta}{\sigma_{oi}^2} \left[\frac{R_i - R0}{\beta_i} \times C^* \right]$$

 σ_m^2 is Variance of the market

 ${\Sigma_{ei}}^2$ is Stock's unsystematic risk

Sharpe Ratio:
$$S = \frac{R_p - R_f}{\sigma_i}$$

Treynor Ratio:
$$T = \frac{R_p - R_f}{\beta_i}$$

Jensen Alpha:
$$Alpha(\alpha) = A(R) - E(R) = R_p - (R_f - \beta(R_m - R_f))$$

Where, Jensen's Alpha is α

A(R) is Actual return

E(R) is Expected Return as per CAPM

Mutual Funds

NAV per unit:

Net Assets of the Scheme)/(No. of units outstanding) Where,

net assets of the scheme =

Market value of Investments +
Receivables + Other accrued income
+ Other assets - Accrued expenses Other payables - Other liabilities

Tracking Error (TE):

$$\sqrt{\frac{\sum (d-\overline{d})^2}{n-1}}$$

Where,

d is Differential return d' or d is Average differential return n = No. of observation

Derivative Analysis and Valuation – Futures

Basis: Spot Price - Futures Price

Annual Compounding:

 $A = P(1+r/100)^{t}$

Where,

A is Compounded amount,P is Principal amount,r is Rate of interest & t is Time period

Interval Compounding:

 $A = P(1+r/n)^{nt}$

Where, n is no of intervals

Continous Compounding:

 $P \times e^{rt} = X$

Where.

e is Epsilon and X is Future Value

Futures Price:

$$F = S \times e^{(r-y)t}$$

Where.

F is Future Value ,S is Spot Value & y is Dividend Yield

Contract Value : Lots size × Futures Price

Beta: $\frac{\Delta \text{ in value of stock}}{\Delta \text{ in value of INDEX}}$

Value of futures contracts to be

hedged : Portfolio Value x Beta of the portfolio

Derivative Analysis and Valuation - Options

Long call payoff : $Max (0, (S_T - X))$ Where,

S_T – Spot price at Maturity Date X – Strike Price

Short call payoff : $Min((X - S_T), 0)$

Long put payoff: Max(0, (X - S_T))

Short put payoff: $Min((S_T - X), 0))$

Delta (△):

Change in the price of the option
Change in the price of the stock

Gamma (y):

Change in the price of the option
Change in delta

Theta (θ) :

Change in the price of the option
Change in time period

Vega (V):

Change in the price of the option
Change in Volatility

Rho (ρ):

Change in the price of the option
Change in Interest rate

Put Call Parity:

 $C + (K \times e^{-rt}) = P + S_0$

Where,

C is Value of call

K is Strike price

e^{-rt} is Present Value

P is Value of Put

S₀ is Spot price

Binomial Model:

Probability:
$$p = \frac{e^{rt} - d}{u - d}$$

Where,

$$u = \frac{Su}{S0}$$

 S_u is spot going up & S_0 is current spot

$$d = \frac{Sd}{S0}$$

S_d is spot going down

Present Value:

$$\frac{(P) \times (u) + (1-P) \times (d)}{e^{rt}}$$

Black Scholes Merton Method

$$C = S_0 e^{-yt} N(d_1) - K e^{-rt} N(d_2)$$

$$d1 = \frac{\ln\left(\frac{S_0}{K}\right) + \left(r - y + \frac{\sigma^2}{2}\right)T}{\sigma\sqrt{T}}$$

$$d_2 = d1 - \sigma\sqrt{T}$$

y = dividend yield

where, C is Call Value, So is Spot

N(d1) - hedge ratio of shares of stock to Options.

K e-rt **N(d2)** – borrowing equivalent to PV of the exercise price times an adjustment factor of N(d2)

Futures price of Commodity:

(S₀)
$$x e^{(r+s-c)t}$$

Where,

S₀ is Spot price

r is Rate of interest

s is Storage cost

c is convenience yield

t is time.

Foreign Exposure and Risk Management

Relationship between direct and indirect quote:

Direct Quote = 1/(Indirect Quote)

% Spread =
$$\frac{\text{Ask-Bid}}{\text{Bid}} \times 100$$

Forward Rate = Spot Rate ± Premium/Discount

Forward Premium % =

Forward Premium Spot Rate x 100

Forward Premium (Annualised):

Forward Premia Spot Rate x \frac{12}{\text{Given Period}} x \frac{100}{\text{Given Period}}

Forward Rate as per Covered Interest Parity:

= Current spot rate (Direct Q) x

1+ Current domestic interest rate

1+ Interest rate of foreign market

Expected Future Spot Rate as per Uncovered Interest Parity:

= Current spot rate (Direct Q) x

1 + Current domestic interest rate

1 + Interest rate of foreign market

Purchasing Power Parity (Absolute Form):

Spot Rate

 $= \alpha x \frac{\text{Price level in domestic market}}{\text{Price level in foreign market}}$

Where,

 α = Sectoral constant for adjustment

Purchasing Power Parity (Relative Form):

 ${\tt Expected \ Spot \ Rate} =$

Current Spot Rate (Direct Q) x

1+Domestic Inflation Rate

1+ Foreign Inflation Rate

International Fisher Effect:

Expected Spot Rate =

Current Spot Rate

1+ Domestic interest rate

1+Interest rate in Foreign market

Intl. Financial Management

Modified IRR i.e MIRR =

n $\sqrt{\frac{FV \text{ (Positive Cash Flows, Reinvestment rate)}}{-PV \text{ (Negative cash Flows, Finance rate)}}}$

Where, n is project life in years.

$$\begin{split} \textbf{APV} &= \ -I_0 + \ \textstyle \sum_{t=1}^n \frac{X_t}{(1+K)^t} + \\ & \sum_{t=1}^n \frac{T_t}{(1+i_d)^t} + \ \textstyle \sum_{t=1}^n \frac{S_t}{(1+i_d)^t} \end{split}$$

Where.

I₀ is Present Value of Investment Outlay

 $\frac{X_t}{(1+K)^t}$ is present value of operating cash flow

 $\frac{T_t}{(1+i_d)^t}$ is present value of Interest Tax shields

 $\frac{S_t}{(1+i_d)^t}$ is present value of Interest subsidies

Int. Rate Risk Management

Settlement amount on FRA

$$\frac{N(RR-FR)\left(\frac{dtm}{DY}\right)}{\left[1+RR\left(\frac{dtm}{DY}\right)\right]}$$

Where,

N is notional principal amount RR is Reference Rate prevailing on the contract settlement date

FR is Agreed-upon Forward Rate

dtm is days of loan (FRA Specified period)

DY is Total number of days (360 or 365 days)

Interest Rate Cap =

(N) max(0,
$$R_A - R_C$$
). $\frac{dt}{Days in year}$

Where,

N is notional principal amount of the agreement,

 R_A is actual spot rate on the reset date

 R_C is cap rate (expressed as a decimal)

dt is the number of days from the interest rate reset date to the payment date

Interest Rate Floor

=(N) max(0,
$$R_F - R_A$$
). $\frac{dt}{Days in year}$

Interest Rate Collar:

Payment = $(N)[max(0, R_A - R_C) - max(0, R_F - R_A)] \cdot \frac{dt}{Days in year}$

Interest Rate Swaps:

Rate Payment = N. (AIC). $\frac{d_t}{360}$

Where,

N is notional principal amount of the agreement,

AIC is All In Cost (Interest rate – fixed or floating)

dt is number of days from the interest rate to the settlement date

Business Valuation

Beta of Assets : $\beta_a = \beta_e \left[\frac{E}{E + D(1 - t)} \right] + C$

$$\beta_d \left[\frac{D (1-t)}{E+D(1-t)} \right]$$

Where,

 β_a – Ungeared or Asset Beta

 β_e – Geared or Equity Beta

 β_d – Debt Beta

E – Equity

D is Debt

t is Tax rate

P/E to Growth Ratio:

$$PEG Ratio = \frac{PE Ratio}{g \times 100}$$

Where,

P is Market Price per share

E is Earnings per share

g is Growth rate of EPS

Enterprise Value:

$$EV = MC + D - C$$

Where.

MC is Market capitalization,
D is debt and C is Total Cash
Equivalents.

Economic Value Added: EVA =

NOPAT — Capital Charge = EBIT (1 — tax rate) — Invested Capital * WACC

Where,

NOPAT = Net Operating Profit After Taxes

EBIT = Earnings before Interest and

WACC = Weighted Average Cost of Capital

Invested Capital = Total Assets minus Non-Interest-Bearing Liabilities

Note: Adjust. EBIT and Invested Capital for non-cash charges (other than depreciation) like provisions for doubtful debts, P&L adjustments.

Market Value Added (MVA):

MVA = MV of E & D – Invested Capital

Miscellaneous

Steps to compute 3(1/0)

- 1. Enter Value 3
- 2. Square root 12 times
- 3. Subtract 1
- 4. Divide by 10 (because 10th Root)
- 5. Add 1
- 6. Press (X =)12 times
- 7. Gen answer 1.1161

E power value on calculator e^{0.16}

- 1. Enter Value 0.16
- 2. Divided by 4096
- 3. Add 1
- 4. X = 12 times
- 5. Final answer =1.17351

Computation of Common Log (base 10) on a Normal Calculator

Eg: Log 1.088235

- 1. Enter Value = 1.088235
- 2. Square root 15 times
- 3. Subtract 1
- 4. Divide by 0.000070271
- 5. Get the log value = 0.03672

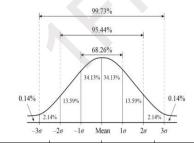
Computation of Natural Log (base e)

Eg: Log 1.088235

- 1. Enter Value = 1.088235
- 2. Square root 12 times
- 3. Subtract 1
- 4. Divide by 0.000244172
- 5. Get the log value = 0.084557

		симі	JLATIVE S	TANDAR	D NORM	AL DISTRI	BUTION 1	TABLE		
Z	0	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
-	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.10	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.20	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6064	0.1064	0.6103	0.6141
0.30	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.40	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.50	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.60	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.70	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.80	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.90	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.00	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.10	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.20	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.30	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.40	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.50	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.60	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.70	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.80	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.90	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.00	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.10	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.20	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.30	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.40	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.50	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.60	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.70	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.80	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.90	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.00	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990

1.645 – 95.0% of cumulative area from left – Lower limit of right 5% Tail
1.960 – 97.5% of cumulative area from left – Lower limit of right 2.5% Tail
2.326 – 99.0% of cumulative area from left – Lower limit of right 1% Tail
2.576 – 99.5% of cumulative area from left – Lower limit of right 0.5% Tail
3.090- 99.9% of cumulative area from left – Lower limit of right 0.1% Tail
3.291- 99.95% of cumulative area from left – Lower limit of right 0.05% Tail



Area under normal curve (Both tails)

1 SD on either side – 68.26% of area under the curve is covered 2 SD on either side – 95.44% of area under the curve is covered 3 SD on either side – 99.73% of area under the curve is covered

1.645 SD on either side – 90% of are under curve is covered 1.960 SD on either side – 95% of are under curve is covered 2.576 SD on either side – 99% of are under curve is covered

T-DISTRIBUTION TABLE

Numbers in each row of the table are values on a t-distribution with (df) degrees of freedom for selected right-tail (greater-than) probabilities (p).



df/p	0.40	0.25	0.10	0.05	0.025	0.01	0.005	0.0005
1	0.324920	1.000000	3.077684	6.313752	12.70620	31.82052	63.65674	636.6192
2	0.288675	0.816497	1.885618	2.919986	4.30265	6.96456	9.92484	31.5991
3	0.276671	0.764892	1.637744	2.353363	3.18245	4.54070	5.84091	12.9240
4	0.270722	0.740697	1.533206	2.131847	2.77645	3.74695	4.60409	8.6103
5	0.267181	0.726687	1.475884	2.015048	2.57058	3.36493	4.03214	6.8688
6	0.264835	0.717558	1.439756	1.943180	2.44691	3.14267	3.70743	5.9588
7	0.263167	0.711142	1.414924	1.894579	2.36462	2.99795	3.49948	5.4079
8	0.261921	0.706387	1.396815	1.859548	2.30600	2.89646	3.35539	5.0413
9	0.260955	0.702722	1.383029	1.833113	2.26216	2.82144	3.24984	4.7809
10	0.260185	0.699812	1.372184	1.812461	2.22814	2.76377	3.16927	4.5869
11	0.259556	0.697445	1.363430	1.795885	2.20099	2.71808	3.10581	4.4370
12	0.259033	0.695483	1.356217	1.782288	2.17881	2.68100	3.05454	43178
13	0.258591	0.693829	1.350171	1.770933	2.16037	2.65031	3.01228	4.2208
14	0.258213	0.692417	1.345030	1.761310	2.14479	2.62449	2.97684	4.1405
15	0.257885	0.691197	1.340606	1.753050	2.13145	2.60248	2.94671	4.0728
16	0.257599	0.690132	1.336757	1.745884	2.11991	2.58349	2.92078	4.0150
17	0.257347	0.689195	1.333379	1.739607	2.10982	2.56693	2.89823	3.9651
18	0.257123	0.688364	1.330391	1.734064	2.10092	2.55238	2.87844	3.9216
19	0.256923	0.687621	1.327728	1.729133	2.09302	2.53948	2.86093	3.8834
20	0.256743	0.686954	1.325341	1.724718	2.08596	2.52798	2.84534	3.8495
21	0.256580	0.686352	1.323188	1.720743	2.07961	2.51765	2.83136	3.8193
22	0.256432	0.685805	1.321237	1.717144	2.07387	2.50832	2.81876	3.7921
23	0.256297	0.685306	1.319460	1.713872	2.06866	2.49987	2.80734	3.7676
24	0.256173	0.684850	1.317836	1.710882	2.06390	2.49216	2.79694	3.7454
25	0.256060	0.684430	1.316345	1.708141	2.05954	2.48511	2.78744	3.7251
26	0.255955	0.684043	1.314972	1.705618	2.05553	2.47863	2.77871	3.7066
27	0.255858	0.683685	1.313703	1.703288	2.05183	2.47266	2.77068	3.6896
28	0.255768	0.683353	1.312527	1.701131	2.04841	2.46714	2.76326	3.6739
29	0.255684	0.683044	1.311434	1.699127	2.04523	2.46202	2.75639	3.6594
30	0.255605	0.682756	1.310415	1.697261	2.04227	2.45726	2.75000	3.6460
z	0.253347	0.674490	1.281552	1.644854	1.95996	2.32635	2.57583	3.2905
CI		-	80%	90%	95%	98%	99%	99.9%

COMMON LOGARITHM TABLE(Base 10)

													Me	ean	Diff	fere	nce		
	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
10	0000	0043	0086	0128	0170	0212	0253	0294	0334	0374	4	8	12	17	21	25	29	33	37
11	0414	0453	0492	0531	0569	0607	0645	0682	0719	0755	4	8	11	15	19	23	26	30	34
12	0792	0828	0864	0899	0934	0969	1004	1038	1072	1106	3	7	10	14	17	21	24	28	31
13	1139	1173	1206	1239	1271	1303	1335	1367	1399	1430	3			13					
14	1461	1492	1523	1553	1584	1614	1644	1673	1703	1732	3	6		12					
15	1761	1790	1818	1847	1875	1903	1931	1959	1987	2014	3	6	8	11	14	17	20	22	25
16	2041	2068	2095	2122	2148	2175	2201	2227	2253	2279	3	5	- 4	11					
17	2304	2330	2355	2380	2405	2430	2455	2480	2504	2529	2	5	7			-	17		
18	2553	2577	2601	2625	2648	2672	2695	2718	2742	2765	2	5	7				16		
19	2788	2810	2833	2856	2878	2900	2923	2945	2967	2989	2	4	7	-			16		
20	3010	3032	3054	3075	3096	3118	3139	3160	3181	3201	2	4	6	0	111	10	15	17	19
21	3222	3243	3263	3284	3304	3324	3345	3365	3385	3404	2	4	6	8	10	12	14	16	18
22	3424	3444	3464	3483	3502	3522	3541	3560	3579	3598	2	4	6	8	10	12	14	15	17
23	3617	3636	3655	3674	3692	3711	3729	3747	3766	3784	2	4	6	7	9	11	13	15	17
24	3802	3820	3838	3856	3874	3892	3909	3927	3945	3962	2	4	5	7	9	11	12	14	16
25	3979	3997	4014	4031	4048	4065	4082	4099	4116	4133	2	3	5	7	9	10	12	14	15
26	4150	4166	4183	4200	4216	4232	4249	4265	4281	4298	2	3	5	7	8	10	11	13	15
27	4314	4330	4346	4362	4378	4393	4409	4425	4440	4456	2	3	5	6	8	9	11	13	14
28	4472	4487	4502	4518	4533	4548	4564	4579	4594	4609	2	3	5	6	8	9	11	12	14
29	4624	4639	4654	4669	4683	4698	4713	4728	4742	4757	1	3	4	6	7	9	10	12	13
30	4771	4786	4800	4814	4829	4843	4857	4871	4886	4900	1	3	4	6	7	9	10	11	13
31	4914	4928	4942	4955	4969	4983	4997	5011	5024	5038	1	3	4	6	7	8	10	11	12
32	5051	5065	5079	5092	5105	5119	5132	5145	5159	5172	1	3	4	5	7	8	9	11	12
33	5185	5198	5211	5224	5237	5250	5263	5276	5289	5302	1	3	4	5	6	8	9	10	12
34	5315	5328	5340	5353	5366	5378	5391	5403	5416	5428	1	3	4	5	6	8	9	10	11
35	5441	5453	5465	5478	5490	5502	5514	5527	5539	5551	1	2	4	5	6	7	9	10	11
36	5563	5575	5587	5566	5611	5623	5635	5647	5658	5670	1	2	4	5	6	7	8	10	11
37	5682	5694	5705	5717	5729	5740	5752	5763	5775	5786	1	2	3	5	6	7	8	9	10
38	5798	5809	5821	5832	5843	5855	5866	5877	5888	5899	1	2	3	5	6	7	8	9	10
39	5911	5922	5933	5944	5955	5966	5977	5988	5999	6010	1	2	3	4	5	7	8	9	10
40	6021	6031	6042	6053	6064	6075	6085	6096	6107	6117	1	2	3	4	5	6	8	9	10
41	6128	6138	6149	6160	6170	6180	6191	6201	6212	6222	1	2	3	4	5	6	7	8	9
42	6232	6243	6253	6263	6274	6284	6294	6304	6314	6325	1	2	3	4	5	6	7	8	9
43	6335	6345	6355	6365	6375	6385	6395	6405	6415	6425	1	2	3	4	5	6	7	8	9
44	6435	6345	6454	6464	6474	6484	6493	6503	6513	6522	1	2	3	4	5	6	7	8	9
45	6532	6542	6551	6561	6571	6580	6590	6599	6609	6618	1	2	3	4	5	6	7	8	9
46	6628	6637	6646	6656	6665	6675	6684	6693	6702	6712	1	2	3	4	5	6	7	7	8
47	6721	6730	6739	6749	6758	6767	6776	6785	6794	6803	1	2	3	4	5	5	6	7	8
48	6812	6821	6830	6839	6848	6857	6866	6875	6884	6893	1	2	3	4	4	5	6	7	8
49	6902	6911	6920	6928	6937	6946	6955	6964	6972	6981	1	2	3	4	4	5	6	7	8
50	6990	6998	7007	7016	7024	7033	7042	7050	7059	7067	1	2	3	3	4	5	6	7	8
51	7076	7084	7093	7101	7110	7118	7126	7135	7143	7152	1	2	3	3	4	5	6	7	8
52	7160	7168	7177	7185	7193	7202	7210	7218	7226	7235	1	2	2	3	4	5	6	7	7
53	7243	7251	7259	7267	7275	7284	7292	7300	7308	7316	1	2	2	3	4	5	6	6	7
54	7324	7332	7340	7348	7356	7364	7372	7380	7388	7396	1	2	2	3	4	5	6	6	7

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55	7404	7412	7419	7427	7435	7443	7451	7459	7466	7474	1	2	2	3	4	5	5	6	7
56	7482	7490	7497	7505	7513	7520	7528	7536	7543	7551	1	2	2	3	4	5	5	6	7
57	7559	7566	7574	7582	7589	7597	7604	7612	7619	7627	1	2	2	3	4	5	5	6	7
58	7634	7642	7649	7657	7664	7672	7679	7686	7694	7701	1	1	2	3	4	4	5	6	7
59	7709	7716	7723	7731	7738	7745	7752	7760	7767	7774	1	1	2	3	4	4	5	6	7
60	7782	7789	7769	7803	7810	7818	7825	7832	7839	7846	1	1	2	3	4	4	5	6	6
61	7853	7860	7868	7875	7882	7889	7896	7903	7910	7917	l ₁	1	2	3	4	4	5	6	6
62	7924	7931	7938	7945	7952	7959	7966	7973	7980	7987	li.	÷	2	3	3	4	5	6	6
63	7993	8000	8007	8014	8021	8028	8035	8041	8048	8055	i.	1	2	3	3	4	5	5	6
64	8062	8069	8075	8082	8089	8096	8102	8109	8116	8122	i	1	2	3	3	4	5	5	6
65	8129	8136	8142	8149	8156	8162	8169	8176	8182	8189	1	1	2	3	3	4	5	5	6
66	8195	8202	8209	8215	8222	8228	8235	8241	8248	8254	l.	4	2	3	3	4	5	5	6
67	8261	8267	8274	8280	8287	8293	8299	8306	8312	8319	li	i	2	3	3	4	5	5	6
68	8325	8331	8338	8344	8351	8357	8363	8370	8376	8382	li.	i	2	3	3	4	4	5	6
69	8388	8395	8401	8407	8414	8420	8426	8432	8439	8445	li.	7	2	2	3	4	4	5	6
70	8451	8457	8463	8470	8476	8482	8488	8494	8500	8506	i	1	2	2	3	4	4	5	6
											1							-	
71	8513	8519	8525	8531	8537	8543	8549	8555	8561	8567	1	1	2	2	3	4	4	5	5
72	8573	8579	8585	8591	8597	8603	8609	8615	8621	8627	Ľ	1	2	2	3	4	4	5	5
73	8633	8639	8645	8651	8657	8663	8669	8675	8681	8686	1	7	2	2	3	4	4	5	5
74	8692	8698	8704	8710	8716	8722	8727	8733	8739	8745	Ľ	1	2	2	3	4	4	5	5
75	8751	8756	8762	8768	8774	8779	8785	8791	8797	8802	1	1	2	2	3	3	4	5	5
76	8808	8814	8820	8825	8831	8837	8842	8848	8854	8859	1	1	2	2	3	3	4	5	5
77	8865	8871	8876	8882	8887	8893	8899	8904	8910	8915	1	1	2	2	3	3	4	4	5
78	8921	8927	8932	8938	8943	8949	8954	8960	8965	8971	1	1	2	2	3	3	4	4	5
79	8976	8982	8987	8993	8998	9004	9009	9015	9020	9025	1	1	2	2	3	3	4	4	5
80	9031	9036	9042	9047	9053	9058	9063	9069	9074	9079	1	1	2	2	3	3	4	4	5
81	9085	9090	9096	9101	9106	9112	9117	9122	9128	9133	1	1	2	2	3	3	4	4	5
82	9138	9143	9149	9154	9159	9165	9170	9175	9180	9186	1	1	2	2	3	3	4	4	5
83	9191	9196	9201	9206	9212	9217	9222	9227	9232	9238	1	1	2	2	3	3	4	4	5
84	9243	9248	9253	9258	9263	9269	9274	9279	9284	9289	1	1	2	2	3	3	4	4	5
85	9294	9299	9304	9309	9315	9320	9325	9330	9335	9340	1	1	2	2	3	3	4	4	5
86	9345	9350	9355	9360	9365	9370	9375	9380	9385	9390	1	1	2	2	3	3	4	4	5
87	9395	9400	9405	9410	9415	9420	9425	9430	9435	9440	ò	1	1	2	2	3	3	4	4
88	9445	9450	9455	9460	9465	9469	9474	9479	9484	9489	0	1	1	2	2	3	3	4	4
89	9494	9499	9504	9509	9513	9518	9523	9528	9533	9538	0	1	1	2	2	3	3	4	4
90	9542	9547	9552	9557	9562	9566	9571	9576	9581	9586	0	1	1	2	2	3	3	4	4
91	9590	9595	9600	9605	9609	9614	9619	9624	9628	9633	0	1	1	2	2	3	3	4	4
92	9638	9643	9647	9652	9657	9661	9666	9671	9675	9680	ŏ	1	1	2	2	3	3	4	4
93	9685	9689	9694	9699	9703	9708	9713	9717	9722	9727	ŏ	i	1	2	2	3	3	4	4
94	9731	9736	9741	9745	9750	9754	9759	9763	9768	9773	ŏ	1	i	2	2	3	3	4	4
95	9777	9782	9786	9791	9795	9800	9805	9809	9814	9818	0	1	1	2	2	3	3	4	4
											_			١.			•	,	
96	9823	9827	9832	9836	9841	9845	9850	9854	9859	9863	0	1	1	2	2	3	3	4	4
97	9868 9912	9872 9917	9877 9921	9881 9926	9886 9930	9890 9934	9894 9939	9899 9843	9903 9948	9908 9952	0	1	1	2	2	3	3	4	4
98 99	9956	9961	9965	9969	9974	9978	9983	9987	9991	9998	0	1	1	2	2	3	3	3	4
33	3330	3301	3303	3303	00/4	3370	9903	9901	3331	3330	ľ		'	-	-	9	0	9	7

COMMON ANTI LOGARITHM TABLE (Base 10)

	0	- 1	2	3	4	5	6	7	8	9			Me	ean d	liffer	ence			
Н											1	2	3	4	5	6	7	8	9
.00	1000	1002	1005	1007	1009	1012	1014	1016	1019	1021	0	0	1	1	1	1	2	2	2
01	1023	1026	1028	1030	1033	1035	1038	1040	1042	1045	0	0	1	1	1	1	2	2	2
12.00	611177.52	100000000000000000000000000000000000000	1052	1054	1057	1059	1062	1064	1067	1069	0	0	î	î	î	î	2		
.02	1047	1050	C00530400C451	100000000000000000000000000000000000000		100000000000000000000000000000000000000	10000000	100 THE R. P. LEWIS CO., LANSING, MICH.	IN THE PROPERTY OF THE PARTY OF	1009	220		1	1	1	271	2	2	2 2
.03	1072	1074	1076	1079	1081	1084	1086	1089	1091	DVC594.45	0	0	1	1	-	1	2		
04	1096	1099	1102	1104	1107	1109	1112	1114	1117	1119	0	8	1	1	1	2	2	2	2
05	1122	1125	1127	1130	1132	1135	1138	1140	1143	1146	0	1	1	1		2	2	2	2
06	1148	1151	1153	1156	1159	1161	1164	1167	1169	1172	0	1	1	1	1	2	2	2	2
07	1175	1178	1180	1183	1186	1189	1191	1194	1197	1199	0	1	1	1	1	2	2	2	2
08	1202	1205	1208	1211	1213	1216	1219	1222	1225	1227	0	1	1	1	1	2 2	2	2	3
.09	1230	1233	1236	1239	1242	1245	1247	1250	1253	1256	0	1	1	1	1	2	2	2	3
10	1259	1262	1265	1268	1271	1274	1276	1279	1282	1285	0	1	1	1	1	2	2	2	3
11	1288	1291	1294	1297	1300	1303	1306	1309	1312	1315	0	1	1	1	2	2	2	2	3
			1324	1327	DOI: DO	1334	02248.01	0.0000000000000000000000000000000000000	100000000000000000000000000000000000000	1346	0		1	1		2	2	2	3
12	1318	1321	Contract of the Contract of th	36709250.758	1330	15.7755	1337	1340	1343	A CONTRACTOR OF THE PARTY OF TH	V90	4	1		2 2 2		2 2 2		
13	1349	1352	1355	1358	1361	1365	1368	1371	1374	1377	0	1	1	1	-	2 2	-	3	3
14	1380	1384	1387	1390	1393	1396	1400	1403	1406	1409	0	8	1	3	2			3	3
15	1413	1416	1419	1422	1426	1429	1432	1435	1439	1442	0	1	1	1	2	2	2	3	3
16	1445	1449	1452	1455	1459	1462	1466	1469	1472	1476	0	1	1	1	2	2	2	3	3
17	1479	1483	1486	1489	1493	1496	1500	1503	1507	1510	0	1	1	1	2	2 2	2	3	3
18	1514	1517	1521	1524	1528	1531	1535	1538	1542	1545	0	1	1	1	2	2	2	3	3
19	1549	1552	1556	1560	1563	1567	1570	1574	1578	1581	0	1	1	1	2	2	3	3	3
20	1585	1589	1592	1596	1600	1603	1607	1611	1614	1618	0	1	1	1	2 2 2 2 2	2	3	3	3
21	1622	1626	1629	1633	1637	1641	1644	1648	1652	1656	0	1	1	2	2	2	3	3	3
22	1660	1663	1667	1671	1675	1679	1683	1687	1690	1694	0	1	1	2	2	2	3	3	3
23	1698	1702	1706	1710	1714	1718	1722	1726	1730	1734	0	1	1	2	2	2	3	3	4
	1738	1742	1746	1750	1754	1758	1762	1766	1770	1774	0	1	1	2	2	2	3	3	4
24 25	1778	1782	1786	1791	1795	1799	1803	1807	1811	1816	0	1	1	2	2	2	3	3	4
	3975	7971		1025		1041	1046	1040	1054	1858		,		2	2	3	3	3	4
26	1820	1824	1828	1832	1837	1841	1845	1849	1854	1901	0	-	-	2		3	3	3	4
27	1862	1866	1871	1875	1879	1884	1888	1892	1897	- 777-771					-	3	3	4	4
28	1905	1910	1914	1919	1923	1928	1932	1936	1941	1945	0			2	2 2 2	3	3	4	4
29	1950	1954	1959	1963	1968	1972	1977	1982	1986	1991	0	1	1	2			3	7	4
30	1995	2000	2004	2009	2014	2018	2023	2028	2032	2037	0	1	1	2	2	3	3	*	4
31	2042	2046	2051	2056	2061	2065	2070	2075	2080	2084	0	1	1	2	2 2	3	3	4	4
32	2089	2094	2099	2104	2109	2113	2118	2123	2128	2133	0	1	1	2	2	3	3	4	4
33	2138	2143	2148	2153	2158	2163	2168	2173	2178	2183	0	1	1	2	2	3	3	4	4
34	2188	2193	2198	2203	2208	2213	2218	2223	2228	2234	1	1	2	2	3	3	4	4	5
35	2239	2244	2249	2254	2259	2265	2270	2275	2280	2286	1	1	2	2	3	3	4	4	5
26	2291	2296	2301	2307	2312	2317	2323	2328	2333	2339	1	1	2	2	3	3	4	4	
36	The second second	2350	2355	2360	2366	2371	2377	2382	2388	2393	li	1	2	2	3	3	4	4	3
37	2344	100000	2410	2415	2421	2427	2432	2438	2443	2449	li	1	2	2	3	3	4	4	-
38	2399	2404	- 0000000	2472	2477	2483	2489	2495	2500	2506	li	i	2	2	3	3	4	5	3
39	2455 2512	2460 2518	2466 2523	2529	2535	2541	2547	2553	2559	2564	li	i	2	2	3	4	4	5	-
.40	2312	2310	2,723	2027		Table Same		1000000	-		1	3		9	-	-			
.41	2570	2576	2582	2588	2594	2600	2606	2612	2618	2624	1	!	2	2	3	4	4	5	-
42	2630	2636	2642	2649	2655	2661	2667	2673	2679	2685	1 1	1	2	1 2	3	4	1 4	-5	
.43	2692	2698	2704	2710	2716	2723	2729	2735	2742	2748	11	1	2	13	3	4	4	5	
.44	2754	2761	2767	2773	2780	2786	2793	2799	2805	2812	1	1	2	3	3	4	4	5	-
45	2818	2825	2831	2838	2844	2851	2858	2864	2871	2877	1	1	2	3	3	4	5	5	
46	2884	2891	2897	2904	2911	2917	2924	2931	2938	2944	1	1	2	3	3	4	5	5	
107	4004	6071	1 4071	0.707	4711	0711	* #7#T	4 4777	# #/JU	B 200 5 5 5			-	100	- 10	1.00		100	

.47	2951	2958	2965	2972	2979	2985	2992	2999	3006	3013	1	1	2	3	3	4	5	5	6
.48	3020	3027	3034	3041	3048	3055	3062	3069	3076	3083	1	1	2	3	4	4	5	6	6
.49	3090	3097	3105	3112	3119	3126	3133	3141	3148	3155	1	1	2	3	4	4	5	6	6
.50	3162	3170	3177	3184	3192	3199	3206	3214	3221	3228	1	1	2	3	4	4	5	6	7
	2100	3110	2000	3101			-			-								3	
.51	3236	3243	3251	3258	3266	3273	3281	3289	3296	3304	1	2	2	3	4	5	5	6	7
	1 THE R. P. LEWIS CO., LANSING, MICH.	CONTRACTOR OF THE PARTY OF THE	3327	3334	3342	3350	3357	3365	3373	3381	1 2		2	3	4	5	5	6	7
.52	3311	3319	-30000		100000000000000000000000000000000000000	- TOTAL - 170	- CO.C.U.	1000000	17775707	100000000000000000000000000000000000000	1 0	2 2	2	3	4	5	6	6	7
.53	3388	3396	3404	3412	3420	3428	3436	3443	3451	3459	1 .						0.55		
.54	3467	3475	3483	3491	3499	3508	3516	3524	3532	3540	1	2	2	3	4	5	6	6	7
.55	3548	3556	3565	3573	3581	3589	3597	3606	3614	3622	1	2	2	3	4	5	6	7	7
	1094	1839	1105	1005	3000	139)	1300	1000											
.56	3631	3639	3648	3656	3664	3673	3681	3690	3698	3707	1	2	3	3	4	5	6	7	8
.57	3715	3724	3733	3741	3750	3758	3767	3776	3784	3793	1	2	3	3	4	5	6	7	8
.58	3802	3811	3819	3828	3837	3846	3855	3864	3873	3882	1	2	3	4	4	5	6	7	8
.59	3890	3899	3908	3917	3926	3936	3945	3954	3963	3972	1	2 2 2	3	4	5	5	6	7	8
.60	3981	3990	3999	4009	4018	4027	4036	4046	4055	4064	1	2	3	4	5	6	6	7	8
	330.	3,70		100	100	35.00	1000	CONS	1000	220%	13	- 6			3				
.61	4074	4083	4093	4102	4111	4121	4130	4140	4150	4159	1	2	3	4	5	6	7	8	9
.62	4169	4178	4188	4198	4207	4217	4227	4236	4246	4256	l i	2	3	4	5	6	7	8	9
1000000	Calaba .	2000	1. VIII. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1.	100000000000000000000000000000000000000	00000	100000000000000000000000000000000000000		2000	4345	4355	I î	2	3	4	5	6	7	8	9
.63	4266	4276	4285	4295	4305	4315	4325	4335	4343	4333	! '	-	3	100	-		1 '		-
.64	4365	4375	4385	4395	4406	4416	4426	4436	4446	4457	1	2	3	4	5	6	17	8	9
.65	4467	4477	4487	4498	4508	4519	4529	4539	4550	4560	Li	2	3	4	5	6	7	8	9
				-						-					-	-	1	-	-
.66	4571	4581	4592	4603	4613	4624	4634	4645	4656	4667	15	2	3	4	5	6	7	9	10
.67	4677	4688	4699	4710	4721	4732	4742	4753	4764	4775	1 7	2	3	4	3	7			
.68	4786	4797	4808	4819	4831	4842	4853	4864	4875	4887	1.3	2			9		8	9	10
.69	4898	4909	4920	4932	4943	4955	3355		1000 C	N. 17722	12	2	3	14	5	7	8	9	10
.70	5012	5023	5035	22222	122/22	-	4966	4977	4989	5000	1 !	2	3	4	5	7	8	9	10
110	3012	3023	2033	5047	5058	5070	5082	5093	5105	5117	1	2	3	4	5	7	8	9	11
.71	5129	5140	5163	****	4124	****		-		1									
	Total Carlo	0.0000000000000000000000000000000000000	5152	5164	5176	5188	5200	5212	5224	5236	1	2	4	5	6	7	8	10	11
.72	5248	5260	5272	5284	5297	5309	5321	5333	5346	5358	1.	2	4	5	6	7	9	10	11
.73	5370	5383	5395	5408	5420	5433	5445	5458	5470	5483	1	3	4	5	6	8	9	10	11
.74	5495	5508	5521	5534	5546	5559	5572	5585	5598	5610	1	3 3	4	5	6	8	9	10	12
.75	5623	5636	5649	5662	5675	5689	5702	5715	5728	5741	1	3	4	5	7	8	9	10	12
1	1000	1	400	123	1952			1	212	10000		- 6	100	1	0	70	1	-	-
.76	5754	5768	5781	5794	5808	5821	5834	5848	5861	5875	1	3	4	15	7	8	9	11	12
.77	5888	5902	5916	5929	5943	5957	5970	5984	5998	6012	l i	3	4	5	7	8	10	11	12
.78	6026	6039	6053	6067	6081	6095	6109	6124	6138	6152	l î	3	4	6	7		10		
.79	6166	6180	6194	6209	6223	6237	6252	6266	6281	6295	I î	3		100	7	8	100	11	13
.80	6310	6324	6339	6353	6368	6383	6397	6412	6427	120000000000000000000000000000000000000	1 :	3	4	6	7	9	10	11	13
100		0021	4007	0000	0.00	0303	0397	0412	0427	6442	1 .	,	4	6	1	9	10	12	13
.81	6457	6471	6486	6501	6516	6531	6546	6561	6822	6500				1	-	2			37
.82	6607	6622	6637	100000000000000000000000000000000000000	0.000	10000000	1000000	0.000	6577	6592	2	3	5	6	-8	9	11	12	14
.83		THE PARTY OF		6653	6668	6683	6699	6714	6730	6745	2	3	5	6	8	9	11	12	14
40.4	6761	6776	6792	6808	6823	6839	6855	6871	6887	6902	2	3	5	6	8	9	11	13	14
.84	6918	6934	6950	6966	6982	6998	7015	7031	7047	7063	2	3	5	6	8	10	11	13	15
.85	7079	7096	7112	7129	7145	7161	7178	7104	1 2211	1 7770	1 4			100		400		3000	430
		1070		1127	7143	7101	11/8	7194	7211	7228	2	3	5	1	8	10	12	13	15
.86	7244	7261	7278	7295	7311	7328	7345	7362	7379	7306	-			-	120	20	4.	-	43
.87	7413	7430	7447	7464	7482	7499	7516	7534	1000000	7396	2	3	5	1	8	10	12	13	15
.88	7586	7603	7621	7638	7656	7674	7691	7709	7551 7727	7568	2	3	5	7	9	10	12	14	16
.89	7762	7780	7798	7816	7834	20000	101719501	Colorada (C)	100000000000000000000000000000000000000	7745	2	4	5	1	9	11	12	14	16
.90	7943	7962	7980	7998	8017	7852	7870	7889	7907	7925	2	4	5	7	9	11	13	14	16
	1		7.700	1330	8017	8035	8054	8072	8091	8110	2	4	6	7	9	11	13	15	17
.91	8128	8147	8166	8185	8204	8222	9241	9340	0220	0300						15			
.92	8318	8337	8356	8375	8395	8414	8241	8260	8279	8299	2	4	6	8	9	11	13	15	17
.93	8511	8531	8551	8570	100000	12000000	8433	8453	8472	8492	2	4	6	8	10	12	14	15	17
.94	8710	8730	8750	8770	8590	8610	8630	8650	8670	8690	2	4	6	8	10	12	14	16	18
.95	8913	8933	8954	22220	8790	8810	8831	8851	8872	8892	2	4	6	8	10	12	14	16	18
1990	0713	6733	0934	8974	8995	9016	9036	9057	9078	9099	2	4	6	8	10	12	15	17	19
.96	9120	9141	9162	9183	9204	9336	0242	0240	0200	02.0		1		100	1000	100			Line
.97	9333	9354	9376	9397	9204	9226	9247	9268	9290	9311	2	4	6	8	11	13	15	17	19
.98	9550	9572	9594	9616	15/00/00/00/00 AV	9441	9462	9484	9506	9528	2	4	7	9	11	13	15	17	20
.99	9772	9795	9817		9638	9661	9683	9705	9727	9750	2	4	7	9	11	13	16	18	20
.57	7112	7195	701/	9840	9863	9886	9908	9931	9954	9977	2	5	7	9	11	14	16	18	20

Natural Logarithm Table (base e)

1n	0	1	2	3	4		6	7	2	9	11	2	3	4	5	6	7	Q	9
1.0			0.0198								_	_	_	_	-	-	_	-	_
	0.0953										_		-	_	-	-		-	_
	0.1823										_		-	_	-	_		-	_
	0.2624										_		22	_	-	_		-	_
	0.3365										_		21			-			
1.5			0.4187								_		19						
	0.4700												18						
1.7			0.5423										17			-			
1.8			0.5988										16						
	0.6419												15					_	
ln	0.0415	1	2	3	4	5	6	7	8	9		2	3			6	7	8	
2.0			0.7031										15						
2.1			0.7514								_	_	14			-	_	-	_
2.2			0.7975								-		13		-				
2.3			0.8416								_	_			-	_		-	
2.4			0.8838									_	12	_	-	_		-	
2.5			0.9243									_	12	_	-	_		-	
2.6			0.9632								_		11	_	-	_			
2.7			1.0006										11		-	_			
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3.2			1.1694								3	6		_	-	_		25	_
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3.4			1.2296								3			_	-	-		23	_
3.5			1.2585				-				3		\vdash	_	-	-		23	_
3.6			1.2865			-					3		\vdash	_	-	_		22	_
3.7			1.3137								3	5	\vdash	_	-	_		21	_
3.8			1.3403								3	5	\vdash	_	-	_		21	_
3.9	1.3610										3	5	\vdash	_	-	_		20	_
ln.	0	1	2	3	4		6	7	8	9	1	2	3	4	5	6	7	8	9
4.0	1.3863	1.3888	1.3913	1.3938			1.4012	1.4036	1.4061	1.4085	2	5	7	10	12	15	17	20	22
4.1	1.4110	1.4134	1.4159	1.4183	1.4207	1.4231	1.4255	1.4279	1.4303	1.4327	2	5		_	-	-		19	_
4.2	1.4351	1.4375	1.4398	1.4422	1.4446	1.4469	1.4493	1.4516	1.4540	1.4563	2	5	7	9	12	14	16	19	21
4.3	1.4586	1.4609	1.4633	1.4656	1.4679	1.4702	1.4725	1.4748	1.4770	1.4793	2	5	7					18	
4.4	1.4816	1.4839	1.4861	1.4884	1.4907	1.4929	1.4951	1.4974	1.4996	1.5019	2	5	7	9	11	14	16	18	20
4.5	1.5041	1.5063	1.5085	1.5107	1.5129	1.5151	1.5173	1.5195	1.5217	1.5239	2	4	7	9	11	13	15	18	20
4.6	1.5261	1.5282	1.5304	1.5326	1.5347	1.5369	1.5390	1.5412	1.5433	1.5454	2	4	6	9	11	13	15	17	19
4.7	1.5476	1.5497	1.5518	1.5539	1.5560	1.5581	1.5602	1.5623	1.5644	1.5665	2	4	6	8	11	13	15	17	19
4.8	1.5686	1.5707	1.5728	1.5748	1.5769	1.5790	1.5810	1.5831	1.5851	1.5872	2	4	6	8	10	12	14	16	19
4.9	1.5892	1.5913	1.5933	1.5953	1.5974	1.5994	1.6014	1.6034	1.6054	1.6074	2	4	6	8	10	12	14	16	18
ln	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
5.0	1.6094	1.6114	1.6134	1.6154	1.6174	1.6194	1.6214	1.6233	1.6253	1.6273	2	4	6	8	10	12	14	16	18
5.1	1.6292	1.6312	1.6332	1.6351	1.6371	1.6390	1.6409	1.6429	1.6448	1.6467	2	4	6	8	10	12	14	16	18
5.2	1,6487	1.6506	1.6525	1.6544	1.6563	1.6582	1.6601	1.6620	1.6639	1.6658	2	4	6	8	10	11	13	15	17
5.3	1.6677	1.6696	1.6715	1.6734	1.6752	1.6771	1.6790	1.6808	1.6827	1.6845	2	4	6	7	9	11	13	15	17
5.4	1.6864	1.6882	1.6901	1.6919	1.6938	1.6956	1.6974	1.6993	1.7011	1.7029	2	4	5	7	9	11	13	15	17
5.5	1.7047	1.7066	1.7084	1.7102	1.7120	1.7138	1.7156	1.7174	1.7192	1.7210	2	4	5	7	9	11	13	14	16
5.6	1.7228	1.7246	1.7263	1.7281	1.7299	1.7317	1.7334	1.7352	1.7370	1.7387	2	4	5	7	9	11	12	14	16
5.7	1.7405	1.7422	1.7440	1.7457	1.7475	1.7492	1.7509	1.7527	1.7544	1.7561	2	3	5	7	9	10	12	14	16
5.8	1.7579	1.7596	1.7613	1.7630	1.7647	1.7664	1.7681	1.7699	1.7716	1.7733	2	3	5	7	9	10	12	14	15
5.9	1.7750	1.7766	1.7783	1.7800	1.7817	1.7834	1.7851	1.7867	1.7884	1.7901	2	3	5	7	8	10	12	13	15

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918	1.79	34	1.7951	1.7967	1.7984	1.8001	1.8017	1.8034	1.8050	1.8066	2	3	5	7	8	10	12	13	1
083	1.80	99	1.8116	1.8132	1.8148	1.8165	1.8181	1.8197	1.8213	1.8229	2	3	5	6	8	10	11	13	1
245	1.82	62	1.8278	1.8294	1.8310	1.8326	1.8342	1.8358	1.8374	1.8390	2	3	5	6	8	10	11	13	1
405	1.84	21	1.8437	1.8453	1.8469	1.8485	1.8500	1.8516	1.8532	1.8547	2	3	5	6	8	9	11	13	1
563	1.85	79	1.8594	1.8610	1.8625	1.8641	1.8656	1.8672	1.8687	1.8703	2	3	5	6	8	9	11	12	1
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282	2.12	94	2.1306	2.1318	2.1330	2.1342	2.1353	2.1365	2.1377	2.1389	1	2	4	5	6	7	8	9	1
401	2.14	12	2.1424	2.1436	2.1448	2.1459	2.1471	2.1483	2.1494	2.1506	1	2	4	5	6	7	8	9	1
518	2.15	29	2.1541	2.1552	2.1564	2.1576	2.1587	2.1599	2.1610	2.1622	1	2	3	5	6	7	8	9	1
633	2.16	45	2.1656	2.1668	2.1679	2.1691	2.1702	2.1713	2.1725	2.1736	1	2	3	5	6	7	8	9	1
748	2.17	59	2.1770	2.1782	2.1793	2.1804	2.1815	2.1827	2.1838	2.1849	1	2	3	5	6	7	8	9	1
861	2.18	72	2.1883	2.1894	2.1905	2.1917	2.1928	2.1939	2.1950	2.1961	1	2	3	4	6	7	8	9	1
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972	2.19	83	2.1994	2.2006	2.2017	2.2028	2.2039	2.2050	2.2061	2.2072	1	2	3	4	6	7	8	9	1
2083	2.20	94	2.2105	2.2116	2.2127	2.2138	2.2148	2.2159	2.2170	2.2181	1	2	3	4	6	7	8	9	1
192	2.22	03	2.2214	2.2225	2.2235	2.2246	2.2257	2.2268	2.2279	2.2289	1	2	3	4	5	6	8	9	1
300	2.23	11	2.2322	2.2332	2.2343	2.2354	2.2364	2.2375	2.2386	2.2396	1	2	3	4	5	6	7	9	1
407	2.24	18	2,2428	2.2439	2.2450	2.2460	2.2471	2.2481	2.2492	2.2502	1	2	3	4	5	6	7	8	1
2513	2.25	23	2.2534	2.2544	2.2555	2.2565	2.2576	2.2586	2.2597	2.2607	1	2	3	4	5	6	7	8	Г
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